DEPARTMENT OF MATHEMATICS
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INTERNAL EXAMINATION - 2021-2022
SEM: V
SUBJECT: MATHEMATICS
PAPER: CC11T

## Full Marks: 10

Answer any one question:
$1 \times 10=10$

1. (a) A Particle moves from rest in a straight line under an attractive force $\mu \times(\text { distance })^{-2}$ per unit mass to a fixed point on the line. If the initial distance from the centre of force be $2 a$, then find the time when the distance will be $a$ from the centre of force.
(b) A particle describes the equiangular spiral $r=a e^{\theta}$ in such a manner that the radial acceleration is zero. Prove that the speed and the magnitude of acceleration are each proportional to $r$.
(c) Eliminate the arbitrary functions and hence obtain the Partial Differential Equations: $x=f(z)+g(y)$

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5+3+2
$$

2. (a) Reduce: $t-s+p-q(1+1 / x)+(z / x)=0$ to canonical form.
(b) Write down the two dimensional wave equation and specify whether it is parabolic or elliptic or hyperbolic partial differential equation.
(c) Solve: $\left(x^{2}-y^{2}-z^{2}\right) p+2 x y q=2 x z$

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5+2+3
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