

**2018**

**CBCS**

**3rd Semester**

**MATHEMATICS**

**PAPER—C7P**

**(Honours)**

**(Practical)**

*Full Marks : 20*

*Time : 2 Hours*

*Program must be written in any programming language or any software. The input/output must be mentioned clearly.*

**Group—A**

Answer any one question 7

*The question must be allotted by lottery*

*[Q.No. 1 to Q.No. 22 will be in Gr-A]*

**Group—B**

Answer any one question 8

*The questions must be allotted by lottery*

*[Q.No. 23 to Q.No. 40 will be in Gr. B]*

*Practical Note Book : 02/Viva : 03*

*(Turn Over)*

**Group—A**Answer any *one* question :

1 × 7

1. Write a program to find the seem of the series  $\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{N}$ . Demonstrate it for  $N = 99, 909$  and 9009.
2. Write a program to enter  $n$  integers into an array and sort them in an ascending order. Test the program for  $n = 0$  and 11.
3. Write a program to find a real root of an equation by Regula falsi method. Demonstrate your program for the equation  $x^x + 2x - 6 = 0$ .
4. Write a program to find a real root of an equation by second method. Demonstrate your program for the equation  $x \sin(x) - 1 = 0$ .
5. Write a program to find a real root of an equation by Bisection method. Demonstrate your program for the equation  $x^3 + x^2 - 1 = 0$
6. Write a program to find a real root of equation by Newton-Raphson method, correct upto 5 decimal places. Demonstrate your program for the equation  $x^5 - 5x^3 + 10x - 14 = 0$ .

7. Write a program to evaluate  $\int_{1.5}^{2.4} (2 \log 2x + x^{13}) dx$  by Simpson  $y^3$  rule taking 100 subintervals.
8. Write a program to evaluate the integral  $\int_0^{1/2} \sqrt{\cos(x)} dx$  numerically by Trapezoidal rule.
9. Write a program to evaluate  $\int_0^1 (23x + e^{\cos x}) dx$  by Weddle's rule taking 12 subintervals.
10. Write a program to evaluate  $\int_0^1 (x^2 + \alpha \cos x) dx$  by Simpson's 1/3 rule taking  $h = 0.1$  and  $\alpha$  is your class roll number.
11. Write a program to find a real root of the equation  $x^3 - 2x - 5 = 0$  by using Method of false position, correct upto three places of decimals.
12. Write a program to estimate the value of  $f(42)$  from the following available Data :

$x$	20	25	30	35	40	45
$f(x)$	354	332	291	260	231	204

13. Write a program to compute the value of  $\int_{0.2}^{1.4} (\sin x - \log x + e^x) dx$  taking  $h = 0.2$  by using Trapezoidal Rule.

14. Write a program to find the root of the following equation using Bisection method Correct to three decimal places:  
 $x^3 - x - 11 = 0$
15. Write a program to find the sum of the series :  
 $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{n}$  for given  $n = 17$ .
16. Write a program to find the root of the equation  $xe^x = \cos x$ , using Secant method Correct upto four places of decimals.
17. Find the solution of algebraic equation  $x^4 - x - 10 = 0$  by Bisection method.
18. Complete a real root of the transcendental equation  $x + \log x - 2 = 0$  correct upto 4 significant figure by iteration method.
19. Find the value of  $\ln 12$  correct upto three decimal places by Newton-Raphson Method.
20. Find a real root of the equation  $x^3 - 2x - 5 = 0$  by Regular Falsi method.
21. Compute  $\int_0^1 \frac{dx}{1+x^2}$  by taking 10 equal sub-intervals by Trapezoidal rule, correct upto 5 significant figures.
22. Evaluate  $\int_0^{\pi/2} (\sqrt{1 - 0.162 \sin^2 x}) dx$  by using Simpson's  $\frac{1}{3}$  rule taking six equal sub-intervals.

## Group—B

Answer any one question

1×8

23. Write a program to find the value of  $\sin(0.175)$  by Lagrange interpolation technique of the following information :

x	0.15	0.17	0.18	0.21	0.23
$\sin x$	0.14944	0.16918	0.18886	0.20846	0.22798

24. Write a program to find the value of  $f(142)$  by Newton Forward interpolation formula of the following information :

x	140	150	160	170	180
$f(x)$	3.685	5.854	6.302	8.072	10.225

25. Write a program to find the value of  $y(0.1)$  from the differential equation  $\frac{dy}{dx} = x + y + 100$ ,  $y(0) = 1.2$  by second order Runge-Kutta method.
26. Write a program to find the value of  $y(0.1)$  and  $y(0.2)$  from the differential equation  $\frac{dy}{dx} = x^2 + y^2$ ,  $y(0) = 1$  by Euler's method.
27. Write a program to find the value of  $y$  when  $x = 0.1$  and  $0.2$  from the differential equation  $\frac{dy}{dx} = x^2 - y$ ,  $y(0) = 1$  by Modified Euler's Method.

33. Given that  $\frac{dy}{dx} = 2 + \sqrt{xy}$  with  $y(1) = 1$ . Write a program to find the approximate value of  $y$  at  $x = 2$  in steps of 0.2, using Modified Euler's method.
34. The area  $A$  (square cm) of a circle of diameter  $d$  (cm) is given for the following values :

$d$	80	85	90	95	100
$A$	5026	5674	6362	7088	7854

Write a program to calculate the area of a circle of diameter 82.5 cm.

35. Write a program to evaluate  $f(9)$  using Lagrange's interpolation formula, given the following set of tabulated values :

$X$	5	7	11	13	17
$f(x)$	150	392	1452	2366	5202

36. Write a program to solve the equations :

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$

by using Gauss Seidal method.

37. A solid of revolution is formed by rotating about the  $x$ -axis, the area between the  $x$ -axis, the lines  $x = 0$  and  $x = 1$

and a curve through the points with the following coordinates :

$x$	0	.25	.50	.75	1
$y$	1	.9896	.9589	.9089	.8415

Write a program to estimate the volume of the solid formed by using Simpson's  $\frac{1}{3}$  Rule.

$$[\text{Volume} = \int_a^b \pi y^2 dx]$$

38. Write a program to solve  $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$  with  $y(0) = 1$  at  $x = 0.2, 0.4$  by using  $R - k$  method of fourth order.
39. Fit a second degree curve to the following data taking  $x$  as independent variables.

$x_i$	1	2	3	4	5	6	7	8	9
$n_i$	2	6	7	8	10	11	11	10	9

40. Solve by Euler's method the ODE  $\frac{dy}{dx} = x - y$ ,  $b(0) = 1$  and  $u = 0.2$ . Find  $y(0.4)$ .