



**JHARGRAM RAJ COLLEGE**  
**DEPARTMENT OF MATHEMATICS**

**MATLAB-1 Practical**

**Course Code: MATSEC01**

**Laboratory Manual:**

**Experiment No. 1**

**Name of the Experiment:** - Find the sum, product, max, min of a list of number in an array, in a sub array without library function.

**Instruction to the Students:**

• **Create an Array:**

- Prompt the user to enter the elements of an array.
- Store these elements in a MATLAB array.

• **Calculate the Sum Without Built-In Functions:**

- Initialize a variable `sum_val` to zero.
- Use a loop to iterate through each element in the array.
- Add each element to `sum_val` to accumulate the total sum.

• **Calculate the Product Without Built-In Functions:**

- Initialize a variable `product_val` to one.
- Use a loop to iterate through each element in the array.
- Multiply each element with `product_val` to get the cumulative product.

• **Find the Maximum Value Without Built-In Functions:**

- Assume the first element of the array is the maximum and store it in `max_val`.
- Loop through the array starting from the second element.
- If any element is greater than `max_val`, update `max_val` with that element.

• **Find the Minimum Value Without Built-In Functions:**

- Assume the first element of the array is the minimum and store it in `min_val`.

- Loop through the array starting from the second element.
- If any element is smaller than `min_val`, update `min_val` with that element.

- **Working with a Subarray:**

- Prompt the user to input the starting and ending indices of a subarray within the main array.
- Apply the above calculations on this subarray by iterating only between the specified indices.

- **Output the Results:**

- Display the calculated sum, product, maximum, and minimum values for both the main array and the selected subarray.

## Experiment No. 2

**Name of the Experiment:** Find a sub matrix of the given matrix

**Instruction to the Students:**

- **Create a Matrix:**

- Prompt the user to enter the size of the matrix (number of rows and columns).
- Prompt the user to enter the elements of the matrix.
- Store these elements in a MATLAB matrix.

- **Specify the Submatrix Boundaries:**

- Prompt the user to enter the starting and ending row indices.
- Prompt the user to enter the starting and ending column indices.
- Ensure these indices are within the bounds of the matrix dimensions.

- **Extract the Submatrix:**

- Use nested loops to iterate through the specified rows and columns.
- Store the values within the specified boundaries into a new matrix.

- **Output the Submatrix:**

- Display the extracted submatrix.

### Experiment No. 3

**Name of the Experiment:** Find the coloumn sum, product, max, min of the given matrix without library function

**Instruction to the Students:**

- **Create a Matrix:**

- Prompt the user to enter the size of the matrix (number of rows and columns).
- Prompt the user to enter the elements of the matrix.
- Store these elements in a MATLAB matrix.

- **Calculate Column-wise Sum Without Built-In Functions:**

- Initialize a row vector `col_sum` with zeros, where each element represents the sum of a column.
- Use nested loops: the outer loop iterates over each column, and the inner loop sums the elements of each column.

- **Calculate Column-wise Product Without Built-In Functions:**

- Initialize a row vector `col_product` with ones, where each element represents the product of a column.
- Use nested loops: the outer loop iterates over each column, and the inner loop multiplies the elements of each column.

- **Find the Maximum of Each Column Without Built-In Functions:**

- Initialize a row vector `col_max` with the first row of the matrix.
- Use nested loops to iterate over each column and compare each element, updating `col_max` if a larger element is found.

- **Find the Minimum of Each Column Without Built-In Functions:**

- Initialize a row vector `col_min` with the first row of the matrix.
- Use nested loops to iterate over each column and compare each element, updating `col_min` if a smaller element is found.

- **Output the Results:**

- Display the calculated sum, product, maximum, and minimum for each column.

## Experiment No. 4

**Name of the Experiment:** Find the row sum, product, max, min of the given matrix without library function

### Instruction to the Students:

- **Create a Matrix:**

- Prompt the user to enter the size of the matrix (number of rows and columns).
- Prompt the user to enter the elements of the matrix.
- Store these elements in a MATLAB matrix.

- **Calculate Row-wise Sum Without Built-In Functions:**

- Initialize a column vector `row_sum` with zeros, where each element represents the sum of a row.
- Use nested loops: the outer loop iterates over each row, and the inner loop sums the elements of each row.

- **Calculate Row-wise Product Without Built-In Functions:**

- Initialize a column vector `row_product` with ones, where each element represents the product of a row.
- Use nested loops: the outer loop iterates over each row, and the inner loop multiplies the elements of each row.

- **Find the Maximum of Each Row Without Built-In Functions:**

- Initialize a column vector `row_max` with the first element of each row.
- Use nested loops to iterate over each row and compare each element, updating `row_max` if a larger element is found.

- **Find the Minimum of Each Row Without Built-In Functions:**

- Initialize a column vector `row_min` with the first element of each row.
- Use nested loops to iterate over each row and compare each element, updating `row_min` if a smaller element is found.

- **Output the Results:**

- Display the calculated sum, product, maximum, and minimum for each row.

## Experiment No. 5

**Name of the Experiment:** Define any transcendental function and then find and show the table of its functional values

**Instruction to the Students:**

- **Define a Transcendental Function:**

- Choose a transcendental function
- Define this function in the program.

- **Specify the Range of Input Values:**

- Prompt the user to enter the start, end, and step size for the range of  $x$ -values over which the function will be evaluated.
- Store these  $x$ -values in a vector.

- **Calculate the Function Values:**

- Use a loop to calculate the function value for each  $x$ -value without directly using MATLAB's built-in transcendental functions
- Stop the series at a reasonable number of terms for accuracy (e.g., 10 terms).

- **Display the Results in a Table:**

- Create a table showing each  $x$ -value alongside its corresponding function value

## Experiment No. 6

**Name of the Experiment:** Plotting of graph of functions  $e^{ax+b}$ ,  $\log(ax + b)$ ,  $\log \frac{1}{(ax+b)}$ ,  $\sin(ax + b)$ ,  $\cos(ax + b)$ ,  $|ax + b|$  and to illustrate the effect of a & b on the graph

### Instruction to the Students:

#### *Step 1: Define Variables and Range*

- Open MATLAB and start a new script.
- Define values for parameters a and b to explore their effects. Start with  $a = 1$  and  $b = 0$ , then try different values of a and b to observe changes.
- Define a range for x, e.g., from -10 to 10, with enough points for smooth plot

#### *Step 2: Define the Functions*

- Define each function in terms of  $(ax + b)$ :
  - Exponential:  $e^{ax+b}$
  - Logarithm:  $\log(ax + b)$
  - Inverse Logarithm:  $\log \frac{1}{(ax+b)}$
  - Sine:  $\sin(ax + b)$
  - Cosine:  $\cos(ax + b)$
  - Absolute Value:  $|ax + b|$

#### *Step 3: MATLAB Code Implementation*

- Use the following MATLAB code to define, compute, and plot each function with initial values of  $a = 1$  and  $b = 0$ . Experiment by changing a and b.

#### *Step 4: Experiment with Different Values of a and b*

- Change a: Observe how the graph's slope changes. For example, setting  $a > 1$  increases steepness, while  $0 < a < 1$  makes the function grow/decay slower.
- Change b: Observe horizontal shifts. A positive b shifts the graph left, while a negative b shifts it right.

## Experiment No. 7

**Name of the Experiment:** Plotting the graphs of polynomial of degree 4 and 5, the derivative graph, the second derivative graph and comparing them

**Instruction to the Students:**

### *Step 1: Define the Polynomials*

1. Open MATLAB and start a new script.
2. Define the 4th-degree polynomial
3. Define the 5th-degree polynomial

### *Step 2: Compute the Derivatives*

1. First Derivative: Use the power rule to compute the first derivatives
2. Second Derivative: Similarly, compute the second derivatives.

### *Step 3: MATLAB Code Implementation*

1. Use the relevant MATLAB code to define, compute, and plot each polynomial and its derivatives.

### *Step 4: Analyze the Graphs*

1. Observe the polynomial graphs and describe the key features, such as the number of peaks, valleys, and general curvature.
2. Compare the first derivatives: Note where each derivative crosses zero, corresponding to peaks and valleys in the polynomial.
3. Examine the second derivatives: Identify regions where the graph is concave up or concave down.

## Experiment No. 8

**Name of the Experiment:** Sketching parametric curves (eg. Trochoid, cycloid, epicycloids, hypocycloid)

**Instruction to the Students:**

### *Step 1: Define the Parameter Range*

- Open MATLAB and start a new script.
- Define the parameter  $t$  with an appropriate range, e.g., from 0 to  $4\pi$  with sufficient points

### *Step 2: Define the Parametric Equations*

- Cycloid: Define  $x$  and  $y$  as:
  - $x = r(t - \sin(t))$

- $y = r(1 - \cos(t))$

Where  $r$  is the radius of the rolling circle.

- Epicycloid: Define  $x$  and  $y$  as:
  - $x = (R + r)\cos(t) - r\cos\left(\frac{R+r}{r} \cdot t\right)$
  - $y = (R + r)\sin(t) - r\sin\left(\frac{R+r}{r} \cdot t\right)$

Where  $R$  is the radius of the fixed circle, and  $r$  is the radius of the rolling circle.

- Hypocycloid: Define  $x$  and  $y$  as:
  - $x = (R - r)\cos(t) + r\cos\left(\frac{R-r}{r} \cdot t\right)$
  - $y = (R - r)\sin(t) - r\sin\left(\frac{R-r}{r} \cdot t\right)$

- Trochoid: Define  $x$  and  $y$  as:
  - $x = r \cdot t - d\sin(t)$
  - $y = r - d\cos(t)$

Where  $d$  is the distance from the point tracing the curve to the center of the rolling circle.

### ***Step 3: MATLAB Code Implementation***

- Use the relevant MATLAB code to define, compute, and plot each parametric curve. Adjust values of  $r$ ,  $R$ , and  $d$  as needed to explore variations in shape.

### ***Step 4: Analyze the Curves***

- Cycloid: Observe the repetitive pattern created by the rolling circle.
- Epicycloid and Hypocycloid: Note how the path changes based on whether the circle rolls on the outside (epicycloid) or inside (hypocycloid).
- Trochoid: Examine how changing  $d$  affects the curve shape, making it closer to a cycloid when  $d = r$

## Experiment No. 9

**Name of the Experiment:** Tracing of conics in cartesian coordinates/polar coordinates

**Instruction to the Students:**

*Step 1: Define Variables and Range*

- Open MATLAB and start a new script.
- Define the range for x and y in Cartesian coordinates

**Step 2: Define Conics in Cartesian Coordinates**

- Write the equation of conics in general form

*Step 3: MATLAB Code Implementation*

- Use the relevant MATLAB code to trace the conic and plot

*Step 4: Analyze the Graphs*

- Display the nature of the conic

## Experiment No. 10

**Name of the Experiment:** Sketching ellipsoid, hyperboloid of one and two sheets, elliptic cone, elliptic cone, elliptic paraboloid and hyperbolic paraboloid using cartesian coordinates

### Instruction to the Students:

#### *Step 1: Define Variables and Range*

- Open MATLAB and start a new script.
- Define the range for  $x, y$  &  $z$  in Cartesian coordinates

#### **Step 2: Define Conics in Cartesian Coordinates**

- Write the equations of ellipsoid, hyperboloid of one and two sheets, elliptic cone, elliptic cone, elliptic paraboloid and hyperbolic paraboloid

#### *Step 3: MATLAB Code Implementation*

- Use the relevant MATLAB code to sketch the conicoids

#### *Step 4: Analyze the Graphs*

- Display the coloured shape of the conicoid

**JHARGRAM RAJ COLLEGE**  
**DEPARTMENT OF MATHEMATICS**

**MATLAB-2 Practical**

**Course Code: MATSEC02**

**Laboratory Manual:**

**Experiment No. 1**

**Name of the Experiment:** Fitting a curve for given data

**Instruction to the Students:**

*Step 1: Define the Data*

- Load or manually define the data points  $(x, y)$ .

*Step 2: Construct the Vandermonde Matrix (A)*

- Construct a Vandermonde matrix A

*Step 3: Solve for Polynomial Coefficients*

- Solve the equation  $A \cdot c = y$  to find the polynomial coefficients c using matrix inversion.

$$\text{Use the equation: } c = (A^T A)^{-1} A^T y$$

*Step 4: Generate the Fitted Curve*

- Use the obtained coefficients to evaluate the polynomial at new points (e.g., for smooth plotting).

Create a fine grid of x-values ( $x_{\text{fit}}$ ) to evaluate the polynomial.

*Step 5: Plot the Data and the Fitted Curve*

- Plot the original data points and the fitted curve using plot

## Experiment No. 2

**Name of the Experiment:** Plotting of given data: Graph plotting, multiple plots, matrix plots, polar plots, 3D plotting (line, surface, mesh and contour) of three dimensional data

### Instruction to the Students:

#### *Step 1: Plotting a 2D Line Plot*

- Create two vectors representing the data to plot

#### *Step 2: Multiple Plots in One Figure*

- Use the subplot function to create multiple plots in one figure

#### *Step 3: Matrix Plot*

- Use the imagesc function to plot a matrix.

#### *Step 4: Polar Plot*

- Create a polar plot to visualize data in polar coordinates

#### *Step 5: 3D Line Plot*

- Use the plot3 function to create a 3D line plot

#### *Step 6: 3D Surface Plot*

- Use the surf function to create a 3D surface plot.

#### *Step 7: 3D Mesh Plot*

- Use the mesh function to create a 3D mesh plot

#### *Step 8: 3D Contour Plot*

- Use the contour function to create a 3D contour plot

### Step 9: Analyze the Results

- **2D Line Plot:** Shows the relationship between two variables.
- **Multiple Plots:** Displays different functions in a single figure for comparison.
- **Matrix Plot:** Visualizes matrix data as color-coded images, often used for heatmaps.
- **Polar Plot:** Visualizes data in polar coordinates, useful for cyclic phenomena.
- **3D Line Plot:** Displays data in 3D space, where each point has X, Y, and Z coordinates.
- **3D Surface Plot:** Visualizes a 3D surface, showing how the surface behaves based on input values.
- **3D Mesh Plot:** Similar to the surface plot, but displays the surface as a mesh grid.
- **3D Contour Plot:** Displays contours of a 3D surface in 2D, representing levels of constant values

### Experiment No. 3

**Name of the Experiment:** Obtaining surface of revolution of curves

**Instruction to the Students:**

***Step 1: Define the Curve to Be Revolved***

- Choose a function or curve that you want to revolve

***Step 2: Create the Parameter Grid***

- Define the range of the curve and the angle of revolution.
  - Let the curve  $y = f(x)$  be revolved around the  $x$ -axis.
  - Create a grid for  $x$  values and  $\theta$  values for the revolution

***Step 3: Parametric Equations for the Surface of Revolution***

- For revolution around the  $x$ -axis:  $Y = f(X) \cdot \cos(\theta)$ ,  $Z = f(X) \cdot \sin(\theta)$  Using the function  $f$  and the parameter grid, calculate the corresponding  $Y$  and  $Z$  values

***Step 4: Plot the Surface***

- Use the surf function to plot the surface of revolution

## Experiment No. 4

**Name of the Experiment:** Find the sum, product, max, min, sort of a list of number in an array, in a sub array using library function

### Instruction to the Students:

#### *Step 1: Define the Array*

- Create an array with a list of numbers

#### *Step 2: Perform Sum Operation*

- Use the sum function to calculate the sum of the array elements

#### *Step 3: Perform Product Operation*

- Use the prod function to calculate the product of the array elements.

#### *Step 4: Find Maximum and Minimum Values*

- Use the max and min functions to find the maximum and minimum values in the array

#### *Step 5: Sort the Array*

- Use the sort function to sort the array in ascending order.

#### *Step 6: Perform Operations on a Sub-array*

- To work with a sub-array, first select a range of elements from the original array.

#### **Step 7: Analyze the Results**

- **Sum and Product:** The sum and product should be straightforward calculations of all the elements in the array or sub-array.
- **Max and Min:** The max and min functions should return the largest and smallest values in the array or sub-array.
- **Sorting:** The sorted array should be in ascending order.
- **Sub-array Operations:** The operations performed on the sub-array should be similar to those performed on the full array, but only for the selected portion of the array.

## Experiment No. 5

**Name of the Experiment:** Find the column sum, product, max, min, sort of the given matrix using library function

### Instruction to the Students:

#### *Step 1: Define the Matrix*

- Create a matrix for which the operations will be performed

#### *Step 2: Column-wise Sum*

- Use the sum function to calculate the sum of elements in each column

#### *Step 3: Column-wise Product*

- Use the prod function to calculate the product of elements in each column

#### *Step 4: Find Maximum and Minimum Values of Each Column*

- Use the max function to find the maximum value in each column.
- Use the min function to find the minimum value in each column

#### *Step 5: Sort Each Column*

- Use the sort function to sort the elements of each column in ascending order

#### **Step 6: Analyze the Results**

- **Column Sum:** The sum of each column is computed, which adds up the elements along each column.
- **Column Product:** The product of the elements in each column is calculated by multiplying the elements of each column.
- **Column Maximum and Minimum:** The max function returns the largest element in each column, while the min function returns the smallest element in each column.
- **Column Sorting:** The sort function sorts the values in each column independently in ascending order.

## Experiment No. 6

**Name of the Experiment:** Find the row sum, product, max, min of the given matrix using library function

**Instruction to the Students:**

### *Step 1: Define the Matrix*

- Create a matrix for which the operations will be performed

### *Step 2: Row-wise Sum*

- Use the sum function to calculate the sum of elements in each Row

### *Step 3: Row-wise Product*

- Use the prod function to calculate the product of elements in each Row

### *Step 4: Find Maximum and Minimum Values of Each Row*

- Use the max function to find the maximum value in each Row.
- Use the min function to find the minimum value in each Row

### *Step 5: Sort Each Row*

- Use the sort function to sort the elements of each Row in ascending order

### **Step 6: Analyze the Results**

- **Row Sum:** The sum of each Row is computed, which adds up the elements along each Row.
- **Row Product:** The product of the elements in each Row is calculated by multiplying the elements of each Row.
- **Row Maximum and Minimum:** The max function returns the largest element in each Row, while the min function returns the smallest element in each Row.
- **Row Sorting:** The sort function sorts the values in each Row independently in ascending order.

## Experiment No. 7

**Name of the Experiment:** Conversion of one number system to another number system among decimal, binary, octal, hexadecimal

**Instruction to the Students:**

*Step 1: Decimal to Binary Conversion*

- To convert a **decimal number** to **binary**, use the dec2bin function

*Step 2: Binary to Decimal Conversion*

- To convert a **binary number** to **decimal**, use the bin2dec function

*Step 3: Decimal to Octal Conversion*

- To convert a **decimal number** to **octal**, use the dec2oct function

*Step 4: Octal to Decimal Conversion*

- To convert an **octal number** to **decimal**, use the oct2dec function

*Step 5: Decimal to Hexadecimal Conversion*

- To convert a **decimal number** to **hexadecimal**, use the dec2hex function

*Step 6: Hexadecimal to Decimal Conversion*

- To convert a **hexadecimal number** to **decimal**, use the hex2dec function

## Experiment No. 8

**Name of the Experiment:** Solution of a square, under determined and over determined system of linear equation

### Instruction to the Students:

#### *Step 1: Square System (Unique Solution)*

- Consider the system of equations

#### *Step 2: Under-Determined System (Infinite Solutions)*

- Consider the system with fewer equations than unknowns

#### *Step 3: Over-Determined System (Least-Squares Solution)*

- Consider the system with more equations than unknowns

### Step 4: Analyze the Results

- **Square system:** If the coefficient matrix  $A$  is invertible, you will get a unique solution.
- **Under-determined system:** The system will have infinitely many solutions, and the solution found is the one that minimizes the least-squares error.
- **Over-determined system:** The system may not have an exact solution, but MATLAB will return the best approximation using least squares

## Experiment No. 9

**Name of the Experiment:** Different problems for root, eigen values and eigen vectors of the matrix

**Instruction to the Students:**

*Step 1: Matrix Input*

- Consider a square matrix

*Step 2: Find the eigen values and eigen vectors of the matrix*

The function `eig` returns a matrix of eigenvectors and a diagonal matrix of eigen values

## **Experiment No. 10**

**Name of the Experiment:** Plotting of recursive sequences

**Instruction to the Students:**

*Step 1: Define the Recursive Sequence*

- Choose a recursive sequence to study.

*Step 2: Plot the Recursive Sequence*

- Plot the sequence to visualize how the terms evolve over time

**Step 3: Analyze the Plot**

- The plot will show the terms of the Fibonacci sequence

## Experiment No. 11

**Name of the Experiment:** Study the convergence of sequences through plotting

**Instruction to the Students:**

### *Step 1: Define the Sequence*

- Choose a sequence  $\{a_n\}$  to study

### *Step 2: Plot the Sequence Terms*

- Plot the terms of the sequence to visualize the behaviour as  $n$  increases

### *Step 3: Analyze the Plot*

- **Convergent Sequence:** If the sequence  $\{a_n\}$  tends towards a finite value as  $n \rightarrow \infty$  the plot will show that the terms approach this value.
- **Divergent Sequence:** If the sequence  $\{a_n\}$  grows without bound or oscillates, the plot will show that the terms keep increasing or oscillating without settling on a finite value.

## Experiment No. 12

**Name of the Experiment:** Verify Bolzano -Weirstrass theorem through plotting of sequences and hence identify convergent sub sequences from the plot

### **Instruction to the Students:**

#### *Step 1: Define the Sequence*

- Define a bounded sequence that oscillates

#### *Step 2: Plot the Sequence*

- Plot the terms of the sequence to visualize how it behaves. The sequence will oscillate, but the values will be bounded.

#### *Step 3: Identify and Plot Convergent Sub sequences*

- A bounded sequence can have sub sequences that converge to different limits

#### **Step 4: Analyze the Plot**

- Verify Bolzano –Weirstrass Theorem

## Experiment No. 13

**Name of the Experiment:** Study the convergence/divergence of infinite series by plotting their sequences of partial sum

**Instruction to the Students:**

### *Step 1: Define the Sequence*

- Choose an infinite series  $\sum a_n$  for which you want to study the convergence/divergence

### *Step 2: Compute the Partial Sums*

- Compute the partial sums using the **cumsum** function.

### *Step 3: Plot the Partial Sums*

- Plot the partial sums of the series to visualize their behaviour as n increases

### *Step 4: Analyze the Plot*

- For a **convergent series**, the partial sums should approach a finite value as n increases. The graph should flatten out after a certain point.
- For a **divergent series**, the partial sums should increase without bound or oscillate as n increases

### **Step 5: Interpret the Results**

- **Convergent Series:** The partial sums should approach a finite value, indicating that the series converges.
- **Divergent Series:** The partial sums should grow without bound, indicating that the series diverges

## Experiment No. 14

**Name of the Experiment:** Cauchy's root test by plotting  $n$ th roots

**Instruction to the Students:**

### *Step 1: Define the Sequence*

- Choose a sequence  $a_n$  for which you want to apply the Root Test

### *Step 2: Compute the $n$ th Root of the Terms*

- Compute the  $n$ -th root of the absolute value of the terms of the sequence.

### *Step 3: Plot the $n$ th Roots of the Terms*

- Plot the  $n$ -th roots of the terms to visualize the behaviour as  $n$  increases

### *Step 4: Analyze the Plot*

- The plot shows how the  $n$ -th roots of the terms behave as  $n$  increases.
- If the  $n$ -th root tends towards a value less than 1, the series is likely to converge.
- If the  $n$ -th root approaches a value greater than 1, the series will diverge.

### **Step 5: Interpret the Results**

- If the  $n$ -th root of  $|a_n|$  tends towards a value less than 1 as  $n$  increases, the series is convergent.
- If the  $n$ -th root is greater than 1, the series diverges.
- If the  $n$ -th root fluctuates around 1, the test is inconclusive.

## Experiment No. 15

**Name of the Experiment:** Ratio test by plotting the ratio of  $n$ th and  $(n+1)$  th term

**Instruction to the Students:**

### *Step 1: Define the Sequence*

- Choose a sequence  $a_n$  for which you want to apply the Ratio Test

### *Step 2: Compute the Ratio of $n$ th and $(n+1)$ th Terms*

- Compute the ratio of the  $(n+1)$ th term to the  $n$ th term

### *Step 3: Plot the Ratio of Terms*

- Plot the ratio of the terms to visualize the behavior of the ratio

### *Step 4: Analyze the Plot*

- The plot shows how the ratio  $\frac{a_{n+1}}{a_n}$  behaves as  $n$  increases.
- If the ratio tends towards a value less than 1, the series is likely to converge.
- If the ratio approaches a value greater than 1, the series will diverge

### **Step 5: Interpret the Results**

- If the ratio  $\frac{a_{n+1}}{a_n}$  is consistently below 1, the series is converging.
- If the ratio exceeds 1 for large values of  $n$ , the series is diverging.
- If the ratio fluctuates around 1, the Ratio Test is inconclusive, and further analysis (such as using other convergence tests) may be needed